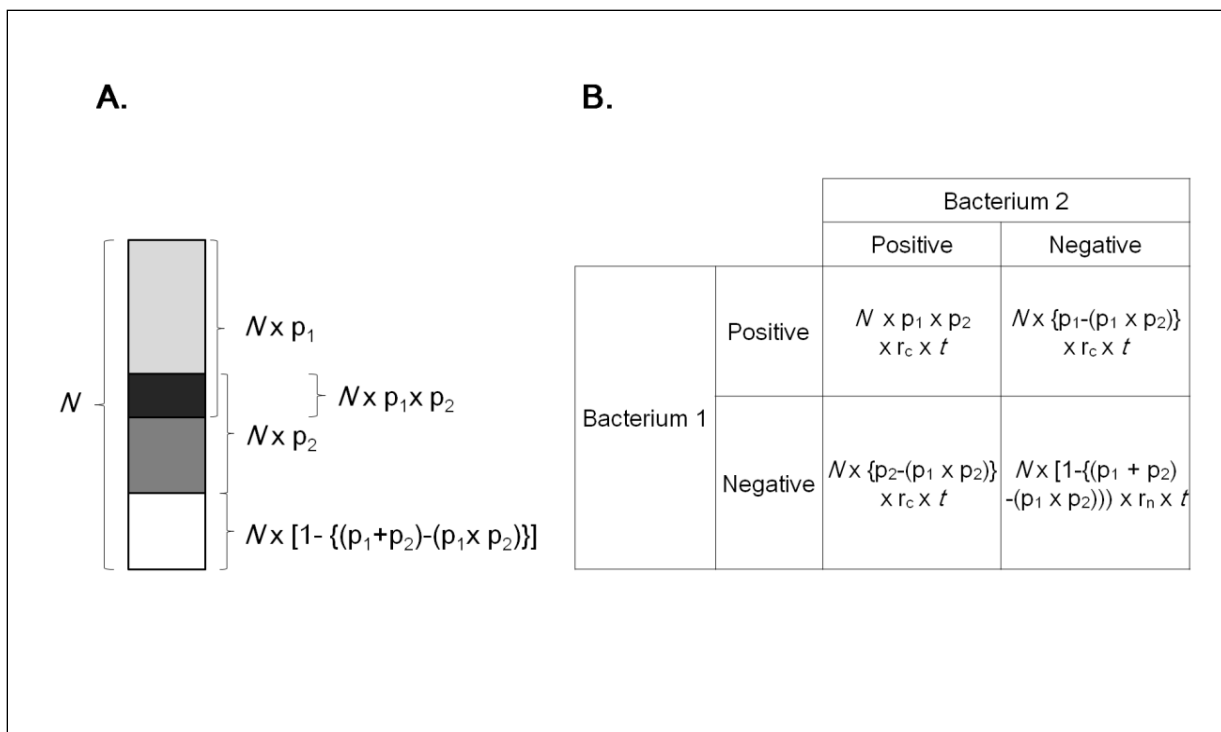


# Nasopharyngeal Bacterial Interactions in Children

## Technical Appendix

Figure. Number of children by bacterial colonization status in a stationary population (A) and cases enrolled during a specified time period (B).



$N$ : the population size

$p_1$ : the prevalence of bacterium 1 colonization

$p_2$ : the prevalence of bacterium 2 colonization

$r_c$ : the risk of enrollment among colonization-positive children

$r_n$ : the risk of enrollment among colonization-negative children

$t$ : a study period

Suppose the colonization of bacterium 1 and of bacterium 2 occur independently in the population.

The odds ratio between bacterium 1 and bacterium 2 in the population ( $OR_{pop}$ ) will be

$$\begin{aligned} OR_{pop} &= \frac{N \times p_1 \times p_2 \times N \times [1 - \{(p_1 + p_2) - (p_1 \times p_2)\}]}{N \times \{p_1 - (p_1 \times p_2)\} \times N \times \{p_2 - (p_1 \times p_2)\}} \\ &= \frac{p_1 \times p_2 - (p_1 \times p_2) \times (p_1 + p_2) - (p_1 \times p_2)^2}{p_1 \times p_2 - (p_1 \times p_2) \times (p_1 + p_2) - (p_1 \times p_2)^2} \\ &= 1 \end{aligned}$$

The OR between bacterium 1 and bacterium 2 in the enrolled cases will be

$$\begin{aligned}
 \text{OR}_{\text{case}} &= \text{OR}_{\text{pop}} \times \frac{r_c \times t \times r_n \times t}{r_c \times t \times r_c \times t} \\
 &= \text{OR}_{\text{pop}} \times \frac{r_n}{r_c} \\
 &= \frac{r_n}{r_c}
 \end{aligned}$$

which is the reciprocal of risk ratio for enrollment (= developing the disease;  $r_c/r_n$ ).