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**AC Impedance Measurements  
Used To Locate Faults  
in Mining Power Cables**



**UNITED STATES DEPARTMENT OF THE INTERIOR**

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**Report of Investigations 8257**

**AC Impedance Measurements  
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**By Richard Hammer and George J. Conroy**



**UNITED STATES DEPARTMENT OF THE INTERIOR  
Cecil D. Andrus, Secretary**

**BUREAU OF MINES**

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# AC IMPEDANCE MEASUREMENTS USED TO LOCATE FAULTS IN MINING POWER CABLES

by

Richard Hammer<sup>1</sup> and George J. Conroy<sup>2</sup>

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## ABSTRACT

Various alternating current (ac) methods can localize faults in mining power cables. Several methods considered by the Bureau of Mines in this report are the Murray loop for short circuits, wherein a bridge provides proportional distance to the fault; capacitance measurements for open conductors; inductance measurements for shorted conductors; phase comparison, high speed recordings of voltage and current in the faulted state are compared with normal voltage and current with the difference being a function of impedance change and impedance change being a function of fault location; and standing wave measurements, detecting the resonance of the length of cable to a fault (either short or open). Portable capacitance bridges are presently available for the second method, and the fourth method is well developed for use on large power distribution systems.

Because it utilizes pulses rather than ac, the time domain reflectometer (TDR) method of fault locating was not included in this investigation. However, a comparative evaluation between this versatile method and the Murray loop might prove advantageous in locating high resistance faults.

## INTRODUCTION

Information was drawn from a literature search on fault location. Of the 32 papers listed in the bibliography, 12 papers had direct relevance to ac methods of fault location.

The following hardware tests were made:

1. The inductance of a shorted wire and capacitance of an open wire were measured under various conditions. The results show some unexplained trends, but were reproducible and linear with distance.

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2. An ac Murray loop fault locator was tested under various conditions. All fault distances were accurate within  $\pm 18$  percent; most results were within  $\pm 7$  percent. Here, also, the errors exhibit unexplained trends.

3. Impedance bridges were tested. The Hewlett-Packard<sup>3</sup> vector impedance meter was found unsuitable for impedance measurements on cables. An Anderson bridge, for measuring inductive reactance, was constructed and tested. It worked, but it was not used for making cable measurements because the General Radio impedance bridge proved to be the more efficient.

## DISCUSSION AND RESULTS

### AC Murray Loop

The Murray loop is an adaptation of the Wheatstone bridge. A simple Wheatstone bridge is shown in figure 1.

In the dc case, when the detector is nulled it can be equated as

$$\frac{R_1}{R_2} = \frac{R_3}{R_4}.$$

In the ac case, the battery is replaced with an ac source and resistors replaced with impedances.

Now at null you have

$$\frac{Z_1}{Z_2} = \frac{Z_3}{Z_4}, \quad (1)$$

where  $Z = R + jx$ ,

$$z = R + j2\pi fL,$$

$f$  is frequency in Hz,

and  $L$  is conductor inductance in henrys.

Since impedance is complex, having two components, two separate conditions must be met to achieve balance. Substituting the complex expressions for the  $Z$ 's in equation 1 yields

$$\frac{Z_1}{Z_2} = \frac{R_1 + jX_1}{R_2 + jX_2} = \frac{R_3 + jX_3}{R_4 + jX_4} = \frac{Z_3}{Z_4},$$

$$(R_1 + jX_1)(R_4 + jX_4) = (R_3 + jX_3)(R_2 + jX_2),$$

and  $R_1 R_4 + j(R_1 X_4 + R_4 X_1) - X_1 X_4 = R_2 R_3 + j(R_2 X_3 + R_3 X_2) - X_2 X_3.$

<sup>3</sup>Reference to specific trade and company names is made for identification only and does not imply endorsement by the Bureau of Mines.

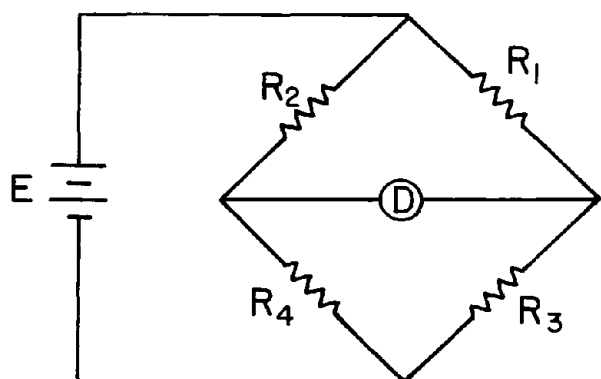


FIGURE 1. - Wheatstone bridge circuit.

Equating first the real components, then the imaginary components, yields equations 2 and 3 as follows:

$$\text{where } R_1 R_4 - X_1 X_4 = R_3 R_2 - X_2 X_3, \quad (2)$$

$$\text{and } R_1 X_4 + R_4 X_1 = R_3 X_2 + R_2 X_3. \quad (3)$$

As a digression, the Murray loop can locate faults of the specific type shown in figure 2.

Phase conductors 1 and 2 must equal each other in resistance and inductance per unit length; that is, they must be the same size wire. The fault resistance can be any magnitude that is significantly less than insulation resistance (less than 10,000 ohms).<sup>4</sup> This is because the fault is connected in series with the power source; it has no impact on the ratios of equation 1.

The faulted cable becomes arms 3 and 4 of the bridge, as shown in figure 3. In this cable, both series resistance and series inductance are linear

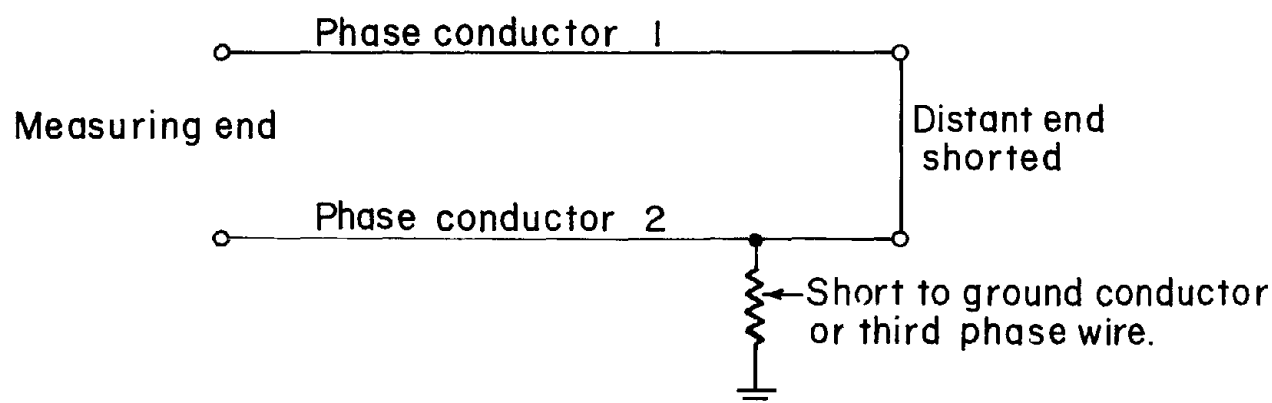


FIGURE 2. - Short circuit fault in mine cable.

<sup>4</sup>See the section headed Murray Loop--Fault Resistance.

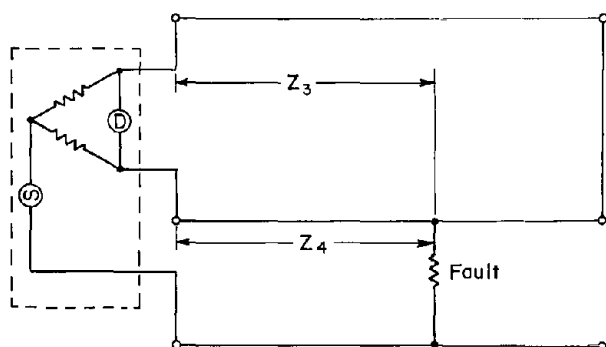


FIGURE 3. - Faulted cable connected to form bridge.

functions of conductor length. This leads to a key assumption regarding the impedances  $Z_3$  and  $Z_4$ :

$$\frac{R_3}{R_4} = \frac{L_3}{L_4}. \quad (4)$$

Now this relation allows the use of simple resistances in arms 1 and 2 of the bridge, because if  $X_1 = X_2 = 0$ , equations 2 and 3 reduce to

$$R_1 R_4 = R_3 R_2,$$

and

$$R_1 X_4 = R_2 X_3,$$

it follows that

$$\frac{R_1}{R_2} = \frac{R_3}{R_4} = \frac{X_3}{X_4} = \frac{L_3}{L_4}. \quad (5)$$

Thus, both the real and imaginary components of equation 1 are balanced with one adjustment--that is, setting the ratio  $R_1 : R_2$ . This is a great simplification.

Conveniently  $R_1$  and  $R_2$  can be made from one slide wire potentiometer,<sup>5</sup> as in figure 4. At null, the distance  $x$  along the slide wire from the tap to end "b" represents the distance along the cable from the fault in conductor 2 to the measuring end (see fig. 2). If null is attained with the tap in the middle ( $x=l$ ) then the fault is located exactly at the distance end of the cable. A null point closer to end "a" ( $x=l$ ) indicates a fault in the other power conductor.

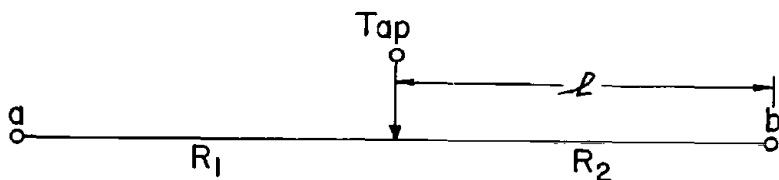


FIGURE 4. - Representation of slide wire potentiometer.

<sup>5</sup>See section headed Impedance of the Bridge Arms--Relative Magnitudes.

The resultant relation is

$$S = \frac{X}{\ell} L,$$

where  $\ell$  = one-half the total length of slide wire,

$S$  = distance to fault along the faulted conductor,

$L$  = cable length,

and  $X$  = shortest distance to an end of the slide wire,

then the faulted conductor is the one connected to the end associated with  $X$ .

The Murray loop has been used as a dc fault locator (16),<sup>6</sup> but the ac application following from assumption 4 and equation 5 was not referenced in the available literature.

#### Assumption 4 Examined

The assumption that  $\frac{R_3}{R_4} = \frac{L_3}{L_4}$  is not strictly true. Mutual inductance is not proportionately distributed between arms 3 and 4 of the bridge. This affects the ratio  $L_3:L_4$ . Note the current flow arrows in the diagram given in figure 5.

By examination

$$\frac{L_3}{L_4} \text{ (ignoring mutual inductance)} \neq \frac{L_3}{L_4} \text{ (actual - incorporating mutual inductance),}$$

and  $\frac{L_3}{L_4} \text{ (actual)} \neq \frac{\text{length of arm 3}}{\text{length of arm 4}}.$

In this case, a simple slide wire will not completely achieve a null. To balance the bridge, a reactive element must be inserted in the slide wire side.

While testing the Murray loop, a decade capacitor was connected so that it could parallel either  $R_1$  or  $R_2$  and achieve balance. If it parallels  $R_1$ , and achieves balance, then equation 6 would hold exactly; otherwise, a broad null would lead to error in fault location.

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<sup>6</sup>Underlined numbers in parentheses refer to items in the bibliography at the end of this report.

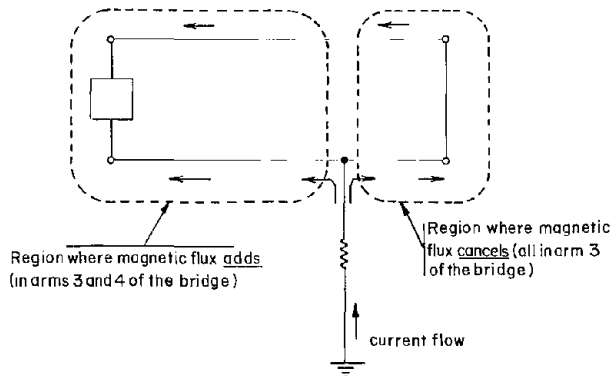


FIGURE 5. - Current flow in bridge circuit.

The experimental data thus obtained do not confirm or refute equation 6. It was impossible to predict which resistor would require the balancing capacitor. The effect of mutual inductance is apparently much less than the effect of noise and such factors as contact resistance that could also affect balance.

The value of capacitance ( $c$ ) used to achieve balance was therefore ignored because it is of secondary importance, and to include its balancing action with regard to the cable's distributed capacitance would have unnecessarily complicated the equation.

#### Murray Loop--Fault Resistance

The Murray loop can locate shorts of resistance less than 10,000 ohms. This is because conduction through the insulation may be ignored as long as it is small compared with conduction through the fault; but when fault conductance is small it must be considered parallel to many other conductances through the insulation to ground. In this case the Murray loop does not work unless appropriate corrections are made (12).

If a Murray loop measurement is made on a cable that is free of shorts or other low resistance paths to ground a null will be obtained, and the fault distance calculated will represent the average location of all conductance through the insulation to ground.

The preceding two paragraphs consider only dc conduction. Obviously there is an ac impedance analog. This study does not reach into that area.

#### Impedance of the Bridge Arms--Relative Magnitudes

In this study  $R_1$  and  $R_2$  were fabricated with a slide wire. A good linear precision wire-wound potentiometer would be easier to use. However, the practicality of a potentiometer may be limited by the following consideration. As stated in references 11 and 18, a Wheatstone bridge works best when its arms have roughly the same resistance. The resistance of the cable loop (arms 3 and 4 of the bridge) is likely to be less than 1 ohm and the slide wire (arms 1 and 2) should be of the same order of magnitude. The slide wire used had about 5 ohms end-to-end. Precision potentiometers of less than 50 ohms

were not found listed in any catalogs and were thus not obtainable during the course of the present investigation.

A 1,000-ohm commercially available precision potentiometer was tested in the ac Murray loop fault locator, and a clear null point was obtained. Therefore, it is possible that proper design would permit satisfactory use of this type of component as a viable replacement for the slide wire, even if lower resistance units are not available.

#### Murray Loop Versus Varley Loop

For trailing cable fault location, the Murray loop is superior to the Varley loop. The Varley loop method requires two separate readings, the Murray loop requires only one. This difference results from the way the methods are designed. The Murray loop method varies the ratio  $R_1:R_2$ ; this indicates  $R_3:R_4$ , which in turn indicated fault distance. The Varley loop uses fixed values for  $R_1$  and  $R_2$  and a rheostat connected in series with the cable. The resultant equations have two unknowns; a solution requires one reading in each of two configurations.

#### Test Procedure

The Murray loop test circuit is shown in figure 6. A short was inserted at one of the lead locations in a 182-ft-long cable. The tap on the 58.2-cm-long slide wire was adjusted to get a minimum signal on the oscilloscope. C and  $S_1$  were adjusted to reduce the signal still further. The slide wire tap was given a final adjustment. Tap distance from node A or B (whichever was closer) was measured. Fault distance in feet was calculated by multiplying tap distance by the factor

$$\text{Ratio} = \frac{L}{\ell} = \frac{182}{0.5 \times 58.2} = 6.25 \frac{\text{ft.}}{\text{cm.}}$$

This procedure was repeated 2X3X4X2 times, that is:

Two fault values, 0 ohm, and 47 ohms.

Three fault locations, 60, 100, and 150 feet.

Four frequencies, 100, 1,000 and 10,000 Hz, and dc.

Two configurations,<sup>7</sup> first with the red phase connected to node A, black connected to node B, and second, the reverse of this. Three additional readings were made at a frequency of 100,000 Hz. The test results are given in tables 1-2.

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<sup>7</sup>Changing the configuration should not change the results. This serves as a double check on the system's symmetry.

TABLE 1.--Murray loop data: Red phase connected to node A, black phase connected to node B

	Fault distance <sup>1</sup>								
	B cm <sup>2</sup>	Results, 60 ft	Capacitor, <sup>3</sup> uf	A cm <sup>4</sup>	Results, 100 ft	Capacitor, <sup>3</sup> uf	B cm <sup>2</sup>	Results, 150 ft	Capacitor, <sup>3</sup> uf
0 ohm short:									
DC.....	10.4	65.0		18.7	116.9		23.8	148.8	
100.....Hz..	10.0	62.5	0	17.9	111.9	2A C	23.4	146.3	2A C
1,000.....Hz..	9.5	59.4	0C	15.1	94.4	8A	21.6	135.1	2.3A
10,000.....Hz..	9.8	61.3	0.14A	15.4	96.3	0.03B	24.6	153.8	0.34A
47 ohm short:									
DC.....	10.2	63.8	0	17.8	111.3		23.6	147.6	
100.....Hz..	10.2	63.8	0.4A	17.7	110.7	0.4B C	23.1	144.5	2B C
1,000.....Hz..	9.4	58.8	0.01A	15.1	94.4	5A	21.4	133.8	2A
10,000.....Hz..	10.0	62.5	0.45A	15.9	99.4	0.8B	24.5	153.2	0.15

<sup>1</sup>Calculate fault distance, tap cm times 6.254.

<sup>2</sup>B cm = tap cm from node B.

<sup>3</sup>Capacitance needed to null:

A indicates capacitor connected between tap and node A.

B indicates capacitor connected between tap and node B.

C indicates broad and vague null with respect to capacitance.

<sup>4</sup>A cm = tap distance in cm along the slide wire from node A.

TABLE 2.--Murray loop data: Red phase connected to node B, black phase connected to node A

	Fault distance <sup>1</sup>								
	A cm <sup>2</sup>	Results, 60 ft	Capacitor, <sup>3</sup> uf	B cm <sup>4</sup>	Results, 100 ft	Capacitor, <sup>3</sup> uf	A cm <sup>2</sup>	Results, 150 ft	Capacitor, <sup>3</sup> uf
0 ohm short:									
DC.....	10.6	66.3		16.9	105.7		24.6	153.8	
100.....Hz..	10.8	67.5	C	16.5	103.2		23.6	147.6	0C
1,000.....Hz..	9.0	56.3	10A	14.5	90.7	10B	19.9	124.5	4A
10,000.....Hz..	9.0	56.3	0.11B	15.8	98.8	0.34A	23.2	145.1	0.63B
100,000.....Hz..	7.6	47.5	0.07B	16.9	105.7	0.03B	23.0	143.8	0.11B
47 ohm short:									
DC.....	10.6	66.3		17.1	106.9		24.6	153.8	
100.....Hz..	10.5	65.7	0C	16.5	103.2	3A C	24.3	152.0	
1,000.....Hz..	8.8	55.0	0C	14.4	90.1	10B C	19.8	123.8	3A
10,000.....Hz..	10.0	62.5	1.6B	15.4	96.3	0.23B	23.6	147.6	1.6B

<sup>1</sup>Calculate fault distance, tap cm times 6.254.

<sup>2</sup>A cm = tap distance in cm along the slide wire from node A.

<sup>3</sup>Capacitance needed to null:

A indicates capacitor connected between tap and node A.

B indicates capacitor connected between tap and node B.

C indicates broad and vague null with respect to capacitance.

<sup>4</sup>B cm = tap cm from node B.



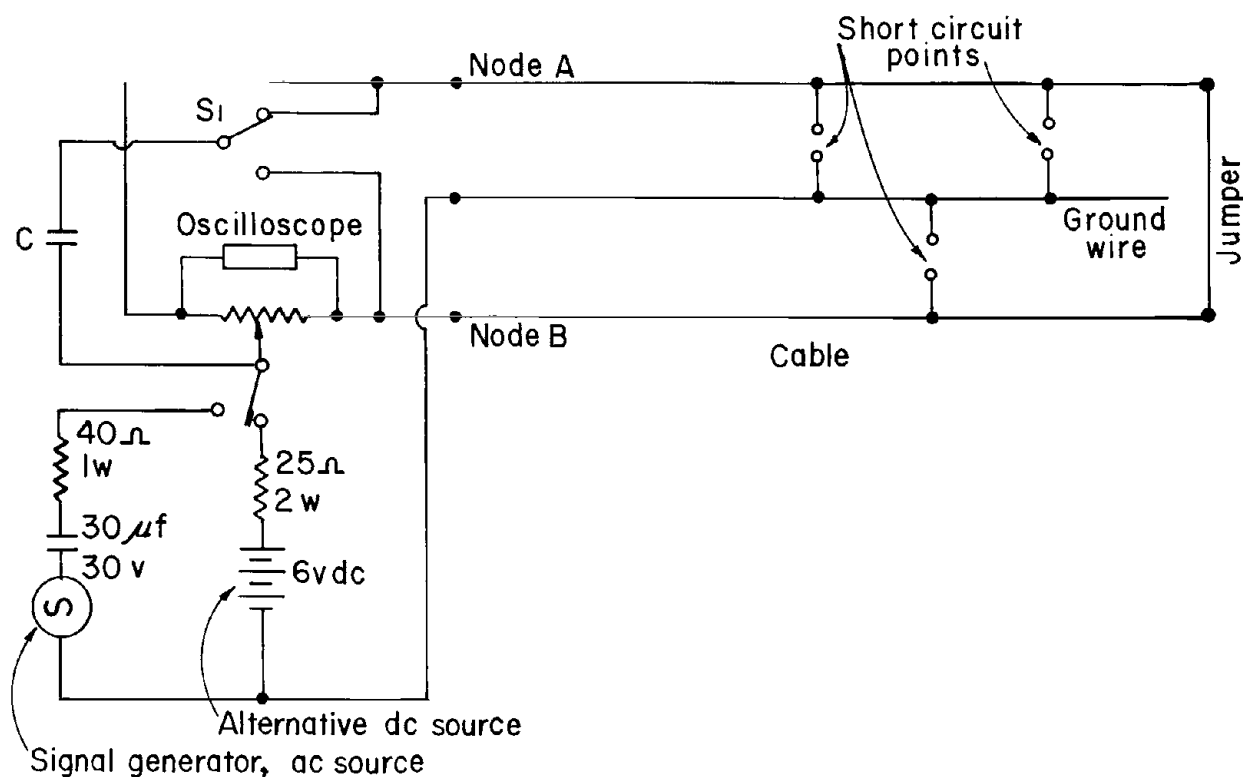


FIGURE 6. - Diagram of Murray loop test circuit.

#### Null Accuracy of the Murray Loop Data

The null point on the slide wire became sharper and more distinct at high frequencies. The exact location of the null point could be established within  $\pm 4$  cm at 100 Hz, whereas at 10,000 Hz, it was found to an accuracy of  $\pm 0.1$  cm. Direct current measurements gave about the same results as did 100 Hz.

#### Cable Inductance

The inductance of a 2-strand No. 18 lamp cord was measured with a General Radio impedance bridge under a variety of circumstances as follows:

1. At each of seven distances to the short, 10, 40, 80, 125, 200, 230, and 250 feet ( $\pm 2$  feet).
2. With two different sized shorts, 0 and 1 ohm.
3. At two frequencies, 1,000 and 6,000 Hz.
4. In two configurations, with the distant end open and with the distant end shorted.

The total cable length was 250 feet ( $\pm 2$  feet).

The General Radio bridge gave two numbers, R and Q. Inductance was calculated as

$$Q = \frac{X}{R},$$

$$X = QR \text{ ohms},$$

$$\omega L = QR \text{ ohms},$$

and

$$L = \frac{QR}{2\pi f} \text{ henrys}.$$

Impedance was calculated as

$$Z = \sqrt{X^2 + R^2}$$

$$Z = \sqrt{(QR)^2 + R^2},$$

and

$$Z = R\sqrt{Q^2 + 1} \text{ ohms}.$$

Phase angle was calculated as

$$\phi = \arctan Q.$$

#### Notes on Cable Inductance Data

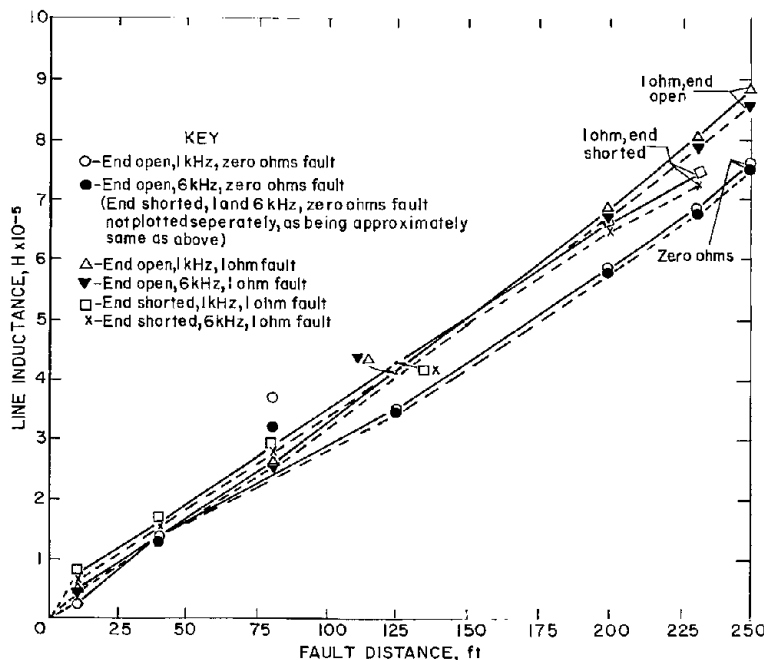


FIGURE 7. - Total inductance versus distance to fault.

Only one graph was made from these data (fig. 7). It displays good linearity, and some unexplained trends, that is, the four straight lines diverge. Inductance is to decrease when frequency increases from 1 to 6 kHz; this may be due to proximity and skin effects (9). No explanation is offered for why L changed significantly as a function of fault resistance. Tabular data is presented in table 3; obviously these data contain enough information for many more studies.

An anomaly occurred at 80 feet for measurements at 1 and 6 kHz, with fault resistance of zero ohm and the cable end open.

TABLE 3.--Inductance of lamp cord data

Short value	Units	Fault distance, feet							
		10		40		80		125	
		1 kHz	6 kHz	1 kHz	6 kHz	1 kHz	6 kHz	1 kHz	6 kHz
0 ohm:									
Open distant end.....	R.....	0.1400	0.1375	0.5288	0.4516	1.074	0.7963	1.676	1.607
	Q*....	.141	.141	.166	.188	.214	.256	.130	.135
	L.....	.314	.309	1.4	1.35	3.658	3.24	3.47	3.45
	Z.....	.141	.180	.536	.681	1.10	1.46	1.69	2.07
	L/ft..	3.15	3.09	3.5	3.38	4.57	4.06	2.77	2.76
	R/ft..	14.00	13.8	13.22	11.3	13.43	9.95	13.41	12.9
	$\phi^{**}$ ...		40.2		48.4		56.9		39.0
Short distant end.....	R.....	.1402	.1375	.5293	.4524	1.077	.7962	1.671	1.605
	Q.....	.140	.141	.166	.187	.214	.256	.130	.135
	L.....	.312	.309	1.4	1.35	3.67	3.24	3.46	3.45
	Z.....	.142	.180	.537	.680	1.10	1.46	1.69	2.07
	$\phi$ .....		40.2		48.3		56.9		39.0
1 ohm									
Open distant end.....	R.....	1.207	1.200	1.582	1.571	2.128	2.083	2.727	2.593
	Q.....	.027	.026	.054	.054	.077	.079	.095	.099
	L.....	.519	.497	1.36	1.35	2.61	2.62	4.12	4.09
	Z.....	1.21	1.21	1.58	1.65	2.13	2.31	2.74	3.02
	L/ft..	5.19	4.97	3.40	3.38	3.26	3.27	3.30	3.27
	$\phi$ .....		8.87	3.09	18.0		25.4		30.7
Short distant end.....	R.....	.9331	.983	1.293	1.331	1.790	1.801	2.320	2.251
	Q.....	.127	.045	.078	.073	.099	.096	.116	.117
	L.....	1.89	.704	1.61	1.55	2.82	2.75	4.28	4.19
	Z.....	.941	1.02	1.30	1.45	1.80	2.08	2.34	2.75
	$\phi$ .....		15.1	4.46	23.7		29.9		35.1
		200		230		250***			
		1 kHz	6 kHz	1 kHz	6 kHz	1 kHz	6 kHz		
0 ohm:									
Open distant end.....	R.....	2.642	2.417	3.044	2.751	3.284	3.006		
	Q*....	.139	.150	.142	.155	.145	.158		
	L.....	5.84	5.77	6.88	6.79	7.58	7.56		
	Z.....	2.67	3.25	3.07	3.757	3.32	4.14		
	L/ft..	2.92	2.89	2.99	2.95	3.03	3.02		
	R/ft..	13.21	12.1	13.23	12.0	13.14	12.0		
	$\phi^{**}$ ...		42.0		42.9		43.5		
Short distant end.....	R.....	2.641	2.415	3.042	2.750				
	Q.....	.139	.150	.142	.155				
	L.....	5.84	5.77	6.87	6.78				
	Z.....	2.67	3.25	3.07	3.76				
	$\phi$ .....		42.0		42.9				
1 ohm:									
Open distant end.....	R.....	3.693	3.389	4.095	3.724	4.303	3.943		
	Q.....	.116	.124	.123	.131	.129	.136		
	L.....	6.82	6.69	8.02	7.76	8.83	8.53		
	Z.....	3.72	4.22	4.13	4.74	4.34	5.09		
	L/ft..	3.41	3.34	3.49	3.38	3.53	3.41		
	$\phi$ .....		36.6		38.2		39.2		
Short distant end.....	R.....	3.047	2.811	3.265	2.955				
	Q.....	.137	.145	.143	.154				
	L.....	6.64	6.49	7.43	7.24				
	Z.....	3.08	3.73	3.30	4.02				
	$\phi$ .....		41.0		42.0				

Units: L = Henrys  $\times 10^{-6}$ ; L/ft = Henrys  $\times 10^{-7}$ ; R/ft = ohms  $\times 10^{-3}$ ;  $\phi$  = degrees.

\*At 6 kHz, Q(actual) = 6XQ(reading). These data are Q(reading). See reference 32.

\*\*Not computed for every reading.

\*\*\*250 feet is the end of the cable. Thus it is meaningless to describe the distant end as open or short.

The one resistor used as a short was measured on the bridge. The results are  $R = 1.075$  ohms and  $Q = 0.003$  ohm.

#### Actual Versus Measured Inductance

The vector impedance of the cable is expressed in terms of a magnitude and a phase angle. It is not satisfactory to assume that the vector is the sum of just two other vector-series resistance and series inductance; instead we must consider four vectors, including shunt capacitance and shunt leakage.

For example, a vector impedance may be measured and found to be as shown in figure 8A. A mistake occurs when the vertical component is all attributed to inductance, as in figure 8B. The truth is more accurately represented by figure 8C.

The General Radio impedance bridge will make this mistake. Its output is expressed in terms of  $L$  and  $Q$  ( $Q = \tan \phi$ ), or in terms of  $R$  and  $Q$ . These

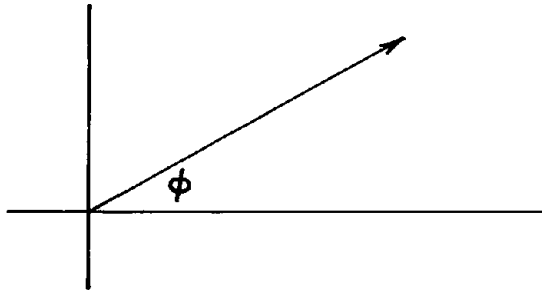


FIGURE 8A. - Vector impedance.

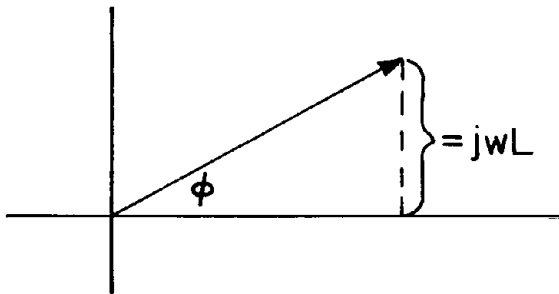


FIGURE 8B. - Reactive component of impedance, neglecting distributed capacitance.

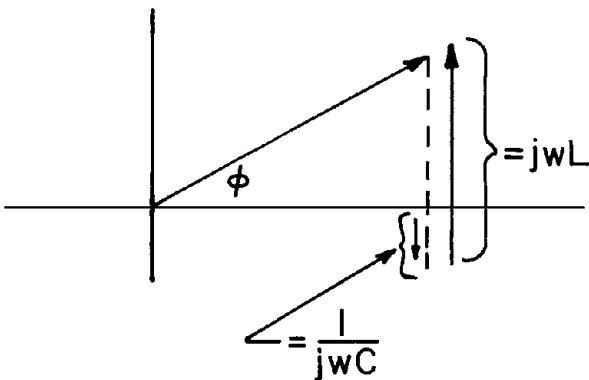


FIGURE 8C. - Reactive components of impedance considering distributed capacitance.

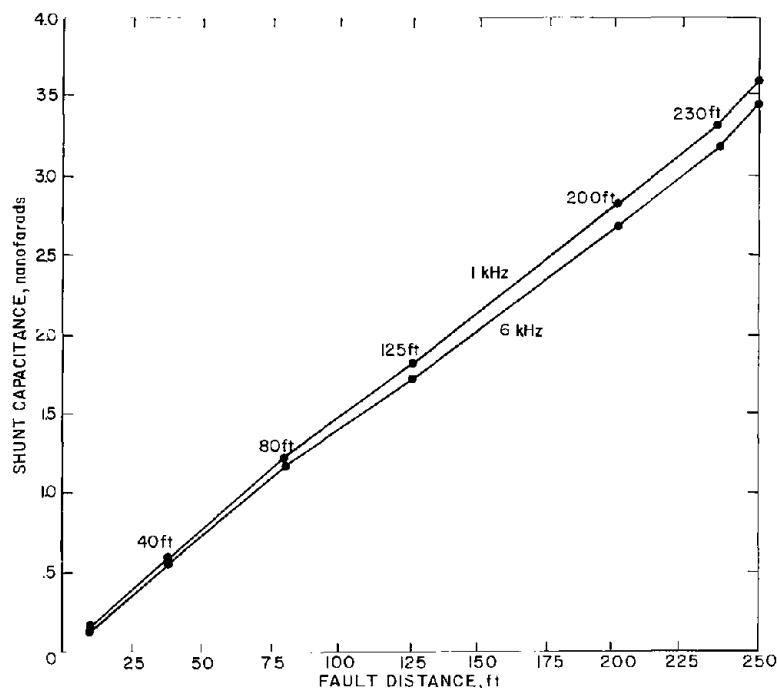


FIGURE 9. - Shunt capacitance versus distance to open circuit fault.

readings of L or R are good only if the inductor measured has no capacitance or leakage. Power cables have capacitance and leakage.

This obviously bears on the experimental measurements of inductance in lamp cord, that were conducted as part of this study. To check, measured values of L were compared with corrected values of L, and the correction factor turned out to be insignificant. In most cases it did not change any of the first three significant digits in the value of L.

Although these particular experimental results were not changed, anyone who intends to measure the "inductance" of a wire

should be aware of this hazard. At higher frequencies it would be more important, at the resonant frequency, for instance  $X_c = X_L$ . Note that the measurement of capacitance in a cable runs into an analogous problem.

#### Capacitance to an Open Fault

The capacitance of the No. 18 lamp cord with an open fault was measured with a General Radio impedance bridge under various conditions: 7 fault distances, 2 frequencies, and 2 configurations with distant end open and distant end shorted.

One plot of these data is shown in figure 9 with the tabulated data presented in table 4. Note that the 1- and 6-kHz lines diverge, more capacitance being measured at the lower frequency. This may be due to permittivity changing with frequency (9).

TABLE 4. - Capacitance of lamp cord data

Parameter	Distance to open fault							
	10 feet		40 feet		80 feet		125 feet	
	1 kHz	6 kHz	1 kHz	6 kHz	1 kHz	6 kHz	1 kHz	6 kHz

## OPEN DISTANT END

C.....	1.495	1.409	5.993	5.720	12.44	11.79	18.11	17.34
D.....	.049	.0106	.0422	.0084	.0402	.0083	.0435	.0088
C/ft.....	1.495	1.409	1.498	1.43	1.555	1.474	1.449	1.387

## SHORT DISTANT END

C.....	1.484	1.405	5.849	5.600	12.09	11.55	18.41	17.36
D.....	.048	.0100	.0457	.0082	.0485	.0088	.0395	.0087

Parameter	Distance to open fault							
	200 feet		230 feet		250 feet			
	1 kHz	6 kHz	1 kHz	6 kHz	1 kHz	6 kHz	1 kHz	6 kHz

## OPEN DISTANT END

C.....	28.43	26.75	33.42	31.89	36.21	34.28
D.....	.049	.0102	.0448	.0088	.0432	.0085
C/ft.....	1.422	1.3388	1.453	1.387	1.45	1.37

## SHORT DISTANT END

C.....	28.84	26.69	33.68	31.97	-	-
D.....	.0453	.01	.0425	.0087	-	-

C = total capacitance, farads  $\times 10^{-10}$ .

D = dissipation factor (dimensionless).

C/ft = capacitance per foot, farads  $\times 10^{-11}$ .

### Requirements for Other AC Fault Locating Methods

Except for the Murray and Varley loops, every ac method for locating faults requires a predetermined knowledge of some physical properties of either the cable under test or an equivalent cable for comparison. The standing wave method requires knowledge of wave propagation velocity. The phase comparison method requires knowledge of the normal phase angle between voltage and current. The capacitance and inductance methods require knowledge of capacitance or inductance per unit length. Other ac methods which require a "prefault" knowledge of cable properties are described in references 10, 17, 27-28. None of these methods are particularly practical because it is unlikely that mining cable properties will be measured before a fault occurs.

### Constraints on Cable End

Most ac methods of fault location require that the distant end of the cable be connected in one particular way. The Murray and Varley loop methods require that the faulted conductor be shorted to another phase conductor at the distant end and that there be no connection (infinite resistance) between the ground conductor and phase wires. The method of measuring inductance requires that the distant end be open. These methods are impractical in situations where the distant end connects to a machine and cannot readily be disconnected.

The standing wave method, on the other hand, does not demand any particular connections at the distant end nor does the method of measuring capacitance to an open end. This latter observation is empirical; it follows from the experience on the lamp cord that was conducted for this study.

### Equations for the Inductance and Capacitance of Two-Conductor Wires

The following equations are based on consideration of the parameters as shown in figure 10. The inductance of the two conductors forming the cable loop is given by

$$L = 4 \times 10^{-7} \left[ 1/4 + \log_n \left( \frac{D}{r} \right) \right] \text{ henrys per meter.}$$

where D = distance between conductor centerlines,

R = radius of conductor.

Source: Page 26 of reference 25.

The capacitance between the two conductors is

$$C = \frac{\pi k}{\log_n \left( \frac{D}{r} \right)} \text{ farads per meter.}$$

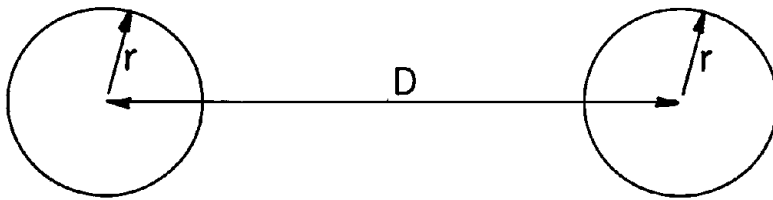


FIGURE 10. - Inductance and capacitance of two-conductor wires.

Where  $K$  is permittivity of the insulation for the lamp cord,  $K$  is assumed to be approximately  $3K_0$ , where  $K_0$  is the permittivity of free space:

$$K_0 = 8.85 \times 10^{-12}.$$

To check validity, these equations were used to calculate the inductance and capacitance of the lamp cord. The dimensions of the No. 18 lamp cord, as measured are

$$D = 0.32 \text{ cm and } r = 0.053 \text{ cm.}$$

Then  $L = 8.19 \times 10^{-7}$  henrys per meter =  $2.5 \times 10^{-7}$  henrys per foot,  
and  $C = 46.39 \times 10^{-12}$  farads per meter =  $14.1 \times 10^{-12}$  farads per foot.

These numbers approximate the experimentally measured inductance and capacitance which were about  $3.2 \times 10^{-7}$  henrys per foot and  $14 \times 10^{-12}$  farads per foot, respectively.

#### CONCLUSIONS

The ac Murray loop method has shown to be a technically feasible approach to trailing cable fault location. To reduce the method to practice, further investigation would be required to accomplish the following objectives:

1. Discover the sources of error in the Murray loop method. With the trends accounted for, it would be possible to attain enough accuracy ( $\pm 5$  per cent) for mining applications.
2. Estimate the retail cost of an ac Murray loop fault locator. The cost would determine whether it could displace, or act as a companion to, TDR devices.
3. Test existing ac bridge fault locators that measure the capacitance or inductance of faulted cables and determine whether or not these devices have any advantages over TDR.
4. Research the properties of transmission lines as they relate to fault location. A technique for locating faults may be found in the dependence of capacitance, inductance, and propagation velocity on frequency.
5. Test the standing wave method on mining cables. This will require the use of radio frequencies, but may be serviceable.



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