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Electrochemical Determination of Thermodynamic Properties of Manganese Sulfate and Cadmium Oxysulfate

By Seth C. Schaefer



UNITED STATES DEPARTMENT OF THE INTERIOR

**Report of Investigations 8809** 

# Electrochemical Determination of Thermodynamic Properties of Manganese Sulfate and Cadmium Oxysulfate

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UNITED STATES DEPARTMENT OF THE INTERIOR James G. Watt, Secretary

**BUREAU OF MINES** Robert C. Horton, Director

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	UNIT OF MEASURE ABBREVIATIONS	USED IN THIS	REPORT
Α	angstrom	kcal	kilocalorie
atm	atmosphere	kcal/mol	kilocalorie per mol
cal/mol•K	calorie per mole, per degree kelvin	min	minute
cal/my	calorie per millivolt	mv	millivolt
h	bour	wt pct	weight percent
ĸ	kelvin		
IX .	KCIVIM		

# ELECTROCHEMICAL DETERMINATION OF THERMODYNAMIC PROPERTIES OF MANGANESE SULFATE AND CADMIUM OXYSULFATE

By Seth C. Schaefer<sup>1</sup>

#### ABSTRACT

The Bureau of Mines investigated thermodynamic properties of MnSO<sub>4</sub> and  $2CdO \cdot CdSO_4$  to obtain basic thermodynamic data applicable to the treatment of mineral concentrates during roasting and sintering processes. Standard Gibbs energies of formation were determined with high-temperature galvanic cells using stabilized  $ZrO_2$  as the electrolyte. Potential measurements were obtained from the cells

Pt, MnSO<sub>4</sub>, MnO, SO<sub>2</sub>(g, 1 atm)//ZrO<sub>2</sub>//O<sub>2</sub>(g, 0.0111 atm), Pt,

Pt, MnSO<sub>4</sub>, Mn<sub>3</sub>O<sub>4</sub>, SO<sub>2</sub>(g, 1 atm)//ZrO<sub>2</sub>//O<sub>2</sub>(g, 0.0112 atm), Pt,

and Pt, 2CdO CdSO<sub>4</sub>, CdO, SO<sub>2</sub>(g, 1 atm)//ZrO<sub>2</sub>//O<sub>2</sub>(g, 0.0092 atm), Pt.

The overall cell reactions are, respectively,

 $2MnO(c) + 2SO_2(g, 1 \text{ atm}) + O_2(g, 0.0111 \text{ atm}) = 2MnSO_4(c),$ 

 $Mn_3O_4(c) + 3SO_2(g, 1 atm) + O_2(g, 0.0112 atm) = 3MnSO_4(c),$ 

and

 $6CdO(c) + 2SO_2(g, 1 \text{ atm}) + O_2(g, 0.0092 \text{ atm}) = 2[2CdO \cdot CdSO_4](c),$ 

where  $0_2^{\prime}$  refers to the indicated partial pressure of oxygen at the reference electrode.

Equilibrium oxygen pressures for the Mn-S-O system were measured and may be expressed as

$$\log pO_2 = -\frac{35,848}{T} + 24.67 \quad (896.5-946.3 \text{ K}),$$
  
$$\log pO_2 = -\frac{46,973}{T} + 36.26 \quad (971.2-1,104.1 \text{ K}),$$
  
$$\log pO_2 = -\frac{44,020}{T} + 33.63 \quad (1,128.6-1,226.8 \text{ K}),$$

and

where  $pO_2$  is the equilibrium oxygen pressure in atmospheres and the temperature (T) is in kelvins. An invariant point was determined at 960 K for the Mn-S-O system, and a phase transition of MnSO<sub>4</sub> was detected at 1,123 K. Similarly, equilibrium oxygen pressures for the Cd-S-O system may be expressed as

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 $\log_{pO_2} = -\frac{39,231}{T} + 27.61$  (1,036.8-1,208.2 K).

Standard Gibbs energies of formation of  $MnSO_4$  and  $2CdO^*CdSO_4$  were derived from these measurements and auxiliary data from the literature and may be expressed as follows:

 $\Delta Gf^{\circ}(MnSO_{4}) = -260.609 + 91.41 \times 10^{-3}T \pm 0.169 \text{ kcal/mol}$  (896.5-946.3 K),

 $\Delta Gf^{\circ}(MnSO_{4}) = -267.958 + 99.25 \times 10^{-3}T \pm 0.176 \text{ kcal/mol} (971.2-1,123 \text{ K}),$ 

$$\Delta Gf^{\circ}(MnSO_{L}) = -262.884 + 94.73 \times 10^{-3}T \pm 0.202 \text{ kcal/mol} (1,123-1,226.8 \text{ K}),$$

and  $\Delta Gf^{\circ}(2Cd0 \cdot CdSO_{4}) = -433.260 + 222.25 \times 10^{-3}T \pm 0.610 \text{ kcal/mol} (1,036.8-1,208.2 \text{ K}).$ 

The standard enthalpy of formation of MnSO4, derived by the third-law method is

 $\Delta Hf_{298}^2 = -257.674 \pm 0.20 \text{ kcal/mol}.$ 

#### INTRODUCTION

Metal sulfates and basic or oxysulfates occur in nature or may be formed when concentrates are treated in unit operations such as roasting and sintering. Selective sulfation has become an important metallurgical process, owing in large part to the availability of the fluid-bed reactor, which permits close control of temperature and gas composition. A scientific approach to sulfation chemistry requires thermodynamic data of sulfation reactions in simple and complex systems.

As a part of its program to expand the base of scientific information required to develop innovative technologies, the Bureau of Mines investigated thermodynamic properties of MnSO<sub>4</sub> (manganese sulfate) and  $2Cd0 \cdot CdO_4$  (cadmium oxysulfate). These data were developed for application in research efforts to maximize recovery of important metals, with minimal energy requirements. The only cadmium mineral of any importance is greenockite, CdS, usually associated with sphalerite in trace amounts. Cadmium is recovered as a by-product in zinc and lead smelting and is used primarily in production of alloys with low melting points. Manganese is an important alloying element in steel production. Since the United States produces only a small percentage of its manganese requirements, a great deal of attention has been given to effective utilization of manganese and improved recovery from its ores. A compilation  $(\underline{11})^2$  of sulfation equilibria shows a need for further study by modern techniques to obtain thermodynamic data for MnSO<sub>4</sub>, and  $2Cd^{\circ}CdSO_4$ , as well as for CdSO<sub>4</sub>, FeSO<sub>4</sub>, and MgSO<sub>4</sub>.

The most commonly used method for determining sulfation equilibria is the measurement of total decomposition pressure within a closed system. However, desorption of moisture from incompletely dried samples causes high pressure readings that result in significant error when the total pressure is small. This method is also subject to slight errors from thermal segregation of the gas species (8, 27). A second method (12, 27) used to study sulfation equilibria is decomposition of the

<sup>2</sup>Underlined numbers in parentheses refer to items in the list of references at the end of this report.

sulfate sample in the presence of substances that fix the oxygen pressure. In this case, the total pressure is no longer subject to error from thermal segregation, and the range of total pressure is adjusted by choice of a metal-metal oxide couple that controls the oxygen pressure over the sulfate. A variety of flow methods (3, 25), which employ a moving gas stream to fix the oxygen pressure, have also been used to study sulfate reactions, but difficulties in achieving equilibrium gas composition at the reaction site often yield erroneous results. Differential thermal analyses

which employ a moving gas stream to fix the oxygen pressure, have also been used to study sulfate reactions, but difficulties in achieving equilibrium gas composition at the reaction site often yield erroneous results. Differential thermal analyses studies (11) provide gualitative data to detect the onset of reactions in a sulfate sample heated at a constant rate in a stream of  $SO_2$  and  $O_2$ . Calorimetric methods have also been used (1, 23-24) to obtain standard-state data for sulfates and oxysulfates of stoichiometric composition. Prediction of chemical behavior by means of calorimetric data can be seriously in error because the properties of the hypothetical standard state may be quite different from the properties that exist in actual equilibrium conditions for complex systems at high temperatures. Recently, electromotive force (emf) techniques using a stabilized  $ZrO_2$  (zirconia) electrolyte were used to investigate metal oxide-metal sulfate equilibria (4-5, 17, 20, 28). The emf method used by the Bureau was specifically designed to obtain accurate equilibrium oxygen dissociation pressures of metal oxide-metal sulfate or metal oxide-metal oxysulfate systems. This technique permits direct determination of the thermodynamic stability of these complex systems and Gibbs energies of formation of sulfates and oxysulfates from their oxides at elevated temperatures.

Application of stabilized  $ZrO_2$  as a selective solid-anion electrolyte has been demonstrated in determining Gibbs energies for cell reactions involving metal-metal oxide systems at elevated temperatures (13). Within the limitation of the ionic domain of stabilized ZrO<sub>2</sub> (22), any equilibrium involving oxygen may be investigated by this technique. The method is based on the measurement of the difference in chemical potential between a reference electrode of known oxygen potential and the oxygen potential of the electrode to be determined. In this investigation, the difference was measured between the oxygen potential of a reference electrode containing a certified standard of  $O_2$  in nitrogen, and the oxygen potential of an electrode consisting of a mixture of a metal oxide and its coexisting sulfate or a metal oxide and its coexisting oxysulfate. The standard states are the saturated coexisting phases. The transport number of oxygen is essentially unity in the range of oxygen potential of this investigation (22). The relationship between the opencircuit potential of the cell and the Gibbs energy change for the actual cell reaction is

$$\Delta G(\text{reaction}) = -nFE, \qquad (1)$$

where  $\Delta G$  is the change in Gibbs energy for the cell reaction, n is the number of electrochemical equivalents in the reaction, F is the Faraday constant (23.061 cal/mv equivalent), and E is the emf in millivolts.

#### EXPERIMENTAL WORK

### Materials

High-purity reagents were obtained from commercial sources and used without further purification. Analyses of these reagents were confirmed, and the results are presented in table 1. Anhydrous-grade  $SO_2$  and a certified standard mixture of  $O_2$  in nitrogen were used. Actual analyses for  $O_2$  in  $O_2$ -nitrogen mixtures were checked by the emf method. The  $O_2$ -nitrogen mixture was dried by passing through Mg(ClO<sub>4</sub>)<sub>2</sub> (magnesium perchlorate), and the SO<sub>2</sub> was dried by passing through a column packed with CaSO<sub>4</sub> (calcium sulfate).

Reagent and impurity elements <sup>1</sup>	wt pct	Reagent and impurity elements <sup>1</sup>	wt pct
MnD:		MnSO, :	
Aluminum	<0.003	Magnesium	<0.001
Magnesium	<.03	Nickel	<.03
Silicon	<.01	Silicon	<.01
Mn <sub>a</sub> D <sub>a</sub> :		Silver	<.003
Aluminum	.07	CdO:	
Copper	<.001	Sodium	<.1
Iron	.13	CdSO, :	
Magnesium	.07	Impurities	ND
Nickel	.06		
Sodium	.12		

TABLE 1. - Impurities detected in reagents

ND No impurities detected.

<sup>1</sup> Impurities not detected by spectrochemical analyses except as noted in the table were Ag, Al, As, B, Ba, Be, Bi, Ca, Cb, Cd, Co, Cr, Cu, Fe, Ga, Ge, Hf, Li, Mg, Mn, Mo, Na, Ni, P, Pb, Pd, Pt, Sb, Si, Ta, Ti, V, W, Y, Zn, and Zr.

NOTE.--X-ray emission and chemical analyses were performed by R. F. Farrell, a research chemist for the analytical laboratory at the Albany Research Center, Bureau of Mines, Albany, OR.

nitrogen were used. Actual analyses for  $0_2$  in  $0_2$ -mitrogen mixtures were checked by the emf method. The  $0_2$ -nitrogen mixture was dried by passing through Mg(Cl0<sub>4</sub>)<sub>2</sub> (magnesium perchlorate), and the SO<sub>2</sub> was dried by passing through a column packed with CaSO<sub>4</sub> (calcium sulfate).

#### Apparatus and Procedure

Internal arrangement of the cell components is illustrated in figure 1.<sup>3</sup> The apparatus, potentiometer, and standardized thermocouple have been described in previous publications (18-19). The reference electrode was a certified standard mixture of  $O_2$  in nitrogen, and the electrode of unknown oxygen potential consisted of a 1:1 molar mixture of MnO plus MnSO<sub>4</sub>, a 1:1 molar mixture of Mn<sub>3</sub>O<sub>4</sub> plus MnSO<sub>4</sub>, or a 1:1 mixture of CdO plus 2CdO<sup>o</sup>CdSO<sub>4</sub>. Measurements were completed in 2 days, following a 12-h stabilization period at 1,040 K. Emf measurements were made with a Keithley model 642 high-input impedance digital electrometer. Reversibility of the cell reaction was checked by approaching equilibrium from above and below a specified temperature. Cell response to temperature change was rapid above 1,000 K, and potentials stabilized within 1 h after a steady-state temperature was reached. Experiments were repeated two or three times for each cell before the cell was dismantled and the electrode removed for X-ray analyses. Reproducibility was checked by obtaining measurements of several separate cells for each determination.

<sup>3</sup>Reference in the figures or text to specific trade names does not imply endorsement by the Bureau of Mines.



FIGURE 1. - High-temperature galvanic cell.

# RESULTS AND DISCUSSION

# MnSO4

The equilibrium oxygen pressures and corresponding Gibbs energy changes for the  $MnO-MnSO_4-SO_2-O_2$  and  $Mn_3O_4-MnSO_4-SO_2-O_2$  systems were determined by measuring the potentials of the reversible cells

Pt, 
$$MnSO_4$$
,  $MnO$ ,  $SO_2(g, 1 atm)//ZrO_2//O_2(g, 0.0111 atm)$ , Pt

and

where the  $0_2^{2}$  refers to the indicated partial pressure of oxygen at the respective reference electrodes. The overall cell reactions are as follows:

. . .

$$2MnO(c) + 2SO_2(g, 1 atm) + O_2(0.0111 atm) = 2MnSO_4(c),$$
 (2)

. . .

and

$$Mn_3O_4(c) + 3SO_2(g, 1 \text{ atm}) + O_2(0.0112 \text{ atm}) = 3MnSO_4(c).$$
 (3)

Potential measurements from the two types of cells that were used for the  $MnSO_{4}$ determination are given in table 2. These results may be expressed as a function of temperature by the least squares equations and standard error of estimate as follows:

$$E = 1,778.15908 - 1.32084T \pm 1.32$$
 (896.5-946.3 K for reaction 2), (4)

$$E = 2,330.01553 - 1.89540T \pm 2.45$$
 (971.2-1,104.1 K for reaction 3), (5)

and  $E = 2,183.52496 - 1.76486T \pm 4.03$  (1,128.6-1,226.8 K for reaction 3), (6)

where E is expressed in millivolts. Smooth emf data from equations 4, 5, and 6 are given in columns 4 and 8 of table 2. Representative emf-versus-temperature data for reactions 2 and 3 are illustrated in figure 2.

The equilibrium oxygen pressure,  $pO_2$ , over MnO + MnSO<sub>4</sub> is determined from the potential measurements for cell reaction 2, and may be expressed as

$$O_{2}^{2}(g, 0.0111 \text{ atm}) = O_{2}(g, \text{ over } MnO + MnSO_{4}).$$
 (7)

The corresponding Gibbs energy change,  $\triangle G$ , for reaction 7 is

$$\Delta G(\text{reaction 7}) = -nFE = RT \ln pO_2 - RT \ln pO_2, \qquad (8)$$

where n is 4, F is the Faraday constant, E is the emf from equation 4, and  $pO_2^-$  is the oxygen pressure at the reference electrode. Pressures are expressed in atmospheres. Rearranging equation 8 and substituting  $pO_2^2$  and E from equation 4 yields

$$\log_{p} pO_{2} = -\frac{35,848}{T} + 24.67 \quad (896.5 - 946.3 \text{ K}). \tag{9}$$

IABLE 2. - Electromotive force (E) of cellsA. Pt, MnSO, MnO, SO, (g, 1 atm)// $ZrO_2//O_2$  (g, 0.0111 atm), PtB. Pt, MnSO, Mn, O, SO, (g, 1 atm)// $ZrO_2//O_2$  (g, 0.0112 atm), Pt

	Tempera-	Ε,	mv		ĭempera-	Ε,	mv
Measurement	ture, K	Measured <sup>1</sup>	Calculated <sup>2</sup>	Measurement	ture, K	Measured	Calculated <sup>2</sup>
1	896.5	593.0 <u>0</u> 0.010	594.02	24	1,039.2	356.23±0.003	360.31
2	898.4	590.91 <sup>±</sup> .055	591.51	25	1,040.7	357.66 <sup>±</sup> .005	357.47
3	898.8	590.61± .005	590.98	26	1,040.7	355.88 .001	357.47
4	899.5	590.47 <sup>±</sup> .005	590.06	27	1,041.5	355.04 <sup>±</sup> .002	355.95
5	899.7	590.53±.020	589.80	28	1,043.1	354.87± .002	352.92
6	914.1	571.58± .025	570.78	29	1,043.1	355.17± .002	352.92
7	919.5	560.95 <sup>±</sup> .015	563.64	30	1,060.0	319.94 .005	320.89
8	920.7	564.70± .005	562.06	31	1,065.3	313.34± .002	310.84
9	921.9	559.46± .010	560.47	32	1,085.4	272.0± .002	272.75
10	922.1	561.29년 .015	560.21	33	1,085.9	271.04 <sup>±</sup> .010	271.80
11	922.4	561.07± .015	559.81	34	1,087.8	267.80± .002	268,20
12	932.4	545.85 .005	546.60	35	1,088.1	269.65± .002	267.63
13	945.5	529.18± .015	529.30	36	1,104.1	236.49± .007	237.30
14	945.7	529.56± .010	529.04	37	1,128.6	189.00± .003	191.71
15	946.3	527.34 .045	528.24	38	1,129.8	189.44± .003	189.59
16	971-2	485.90± .003	489.20	39	1,131.1	193.85± .005	187.29
17	974.2	486.6丈 .003	483.52	40	1,146.7	155.4¢ .001	159.76
18	993.2	444.01± .002	447.50	41	1,172.3	113.24± .005	114.58
19	995.7	441.97± .002	442.76	42	1,210.0	46.22± .001	48.05
20	997.0	443.56± .002	440.30	43	1,211.1	48.51± .003	46.11
21	997.6	441.67±.004	439.16	44	1,213.1	47.3丈 .003	42.58
22	1,016.9	399.32±.002	402.58	45	1,226.8	15.03 <sup>±</sup> .013	18.40
23	1,020.2	399.64 <sup>±</sup> .001	396.33				

 $^1\,\text{Average}$  of 2 measurements taken at 20-min intervals and corrected for cell calibration.  $^2\,\text{Calculated}$  from equations:

E = 1,778.15908- 1.32084ĭ  $\pm$  1.32 (896.5-946.3 K), E = 2,330.01553- 1.89540ĭ  $\pm$  2.45 (971.2-1,104.1 K), and E = 2,183.52496- 1.76486ĭ  $\pm$  4.03 (1,128.6-1,226.8 K).

and

NOTE.--Cell A was used for measurements for reaction 2 in temperature range 896.5 to 946.3 K (measurements 1-15); cell B was used for reaction 3 in temperature range 971.2 to 1,226.8 K (measurements 16-45).

The equilibrium oxygen pressure,  $pO_2$ , over  $Mn_3O_4 + MnSO_4$  for reaction 3 is obtained by the method previously described for reaction 7. Rearranging equation 8 and substituting the value of  $pO_2$ , the partial pressure at the reference electrode, and E for reaction 3 from equations 5 and 6 respectively, yields

$$\log pO_2 = -\frac{46,973}{\pi} + 36.26 \quad (971.2 - 1,104.1 \text{ K}), \tag{10}$$

 $\log pO_2 = -\frac{44,020}{T} + 33.63 \quad (1,128.6-1,226.8 \text{ K}). \tag{11}$ 

Figure 3 illustrates the thermodynamic stability of that portion of the Mn-S-O system where MnO coexists with  $MnSO_4$  in the temperature range 896.5 to 946.3 K and  $Mn_3O_4$  coexists with  $MnSO_4$  in the temperature range 971.2 to 1,226.8 K. An invariant



FIGURE 2. - Electromotive force (E) versus temperature for MnSO<sub>4</sub> reactions.

point was determined at 960 K for the Mn-S-O system, and a transition of MnSO<sub>4</sub> was detected at 1,123 K. Reaction 7 and equation 8 are independent relationships that are applicable to any equilibrium involving oxygen. These values of  $pO_2$  at the reaction site are the key for computing the standard Gibbs energy changes for the reactions

$$2MnO(c) + 2SO_2(g) + O_2(g) = 2MnSO_4(c)$$
(12)

and

and

$$Mn_{3}O_{4}(c) + 3SO_{2}(g) + O_{2}(g) = 3MnSO_{4}(c)$$
(13)

from the relationships

$$\Delta G^{\circ}(\text{reaction 12}) = -RT \ln K_{12} = RT \ln pO_2 + 2RT \ln pSO_2$$
(14)

$$\Delta G^{\circ}(\text{reaction 13}) = -RT \ln K_{13} = RT \ln pO_2 + 3RT \ln pSO_2, \quad (15)$$



FIGURE 3. - Equilibrium diagram for MnO-MnSO<sub>4</sub>-SO<sub>2</sub>-O<sub>2</sub> and Mn<sub>3</sub>O<sub>4</sub>-MnSO<sub>4</sub>-SO<sub>2</sub>-O<sub>2</sub> systems.

where  $K_{12}$  and  $K_{13}$  are the equilibrium constants,  $pO_2$  is the equilibrium oxygen pressure,  $pSO_2$  is the equilibrium  $SO_2$  pressure for reactions 12 and 13, respectively, and the condensed phases are assumed to have unit activity. The equilibrium oxygen pressure is obtained from equation 9 for reaction 12 and from equation 10 or 11 for reaction 13. Resolution of the partial pressures of  $SO_2$  at the reaction site for reactions 12 and 13 involves evaluation of the following equilibrium reaction and relationships:

$$SO_3(g) = SO_2(g) + 0.5 O_2(g),$$
 (16)

$$K_{p,16} = \frac{pSO_2(pO_2)^{0.5}}{pSO_3},$$
 (17)

$$P_{total} = pSO_3 + pSO_2 + pO_2,$$
 (18)

where  $P_{total}$  is the total pressure and pSO<sub>3</sub>, pSO<sub>2</sub>, and pO<sub>2</sub> are the partial pressures of the gaseous components in atmospheres. The SO<sub>2</sub> pressure at the interface of MnO-MnSO<sub>4</sub> or Mn<sub>3</sub>O<sub>4</sub>-MnSO<sub>4</sub> electrodes and the electrolyte was calculated by combining equations 17 and 18 to yield

$$pSO_2 = \frac{P_{total} - PO_2}{1 + (PO_2)^{0.5}/K_{p_1}^{16}},$$
 (19)

where  $K_{0,16}$  is the equilibrium constant for reaction 16 (equation 17), based on auxiliary data from the literature (15).

The average total pressure of the system is 0.99307 atm for the MnO-MnSO<sub>4</sub>-SO<sub>2</sub>-O<sub>2</sub> equilibrium and 0.99917 atm for the Mn<sub>3</sub>O<sub>4</sub>-MnSO<sub>4</sub>-SO<sub>2</sub>-O<sub>2</sub> measurements. Calculations show that pSO<sub>2</sub> is 0.99307 atm in the temperature range 896.5 to 946.3 K. For the latter system, pSO<sub>2</sub> is 0.99917 atm at 971.2 K, 0.99873 atm at 1,104.1 K, 0.99817 atm at 1,128.6, and 0.97802 atm at 1,226.8 K. Consequently, in the temperature range of this investigation, the standard Gibbs energies for reactions 12 and 13, as given by equations 14 and 15, are not appreciably affected by the slight variation of pSO<sub>2</sub> from standard conditions.

Results of these calculations and those of previous investigators are presented in tables 3 and 4. As noted in table 3, the results from this investigation for reaction 12 are more negative than those derived from calorimetric data (14). Considerable disagreement is also noted in table 4 between the results of this investigation and those based on calorimetric measurements (11, 14) for reaction 13. Discrepancies in the data from the various investigations for reaction 13 are illustrated in figure 4.

TABLE 3. - Standard Gibbs energy change  $(-\Delta G^{\circ})$  for  $2MnO(c) + 2SO_2(g) + O_2(g) = 2MnSO_4(c)$ (kilocalories per mole  $O_2$ )

Temperature, K	Mah (calorimetry)	This investigation
896.5	57.320	62.840
900.0	56.858	62.444
946.3	50.742	57.219

TABLE 4. - Standard Gibbs energy change  $(-\Delta G^{\circ})$  for  $Mn_3O_{4}(c) + 3SO_{2}(g) + O_{2}(g) = 3MnSO_{4}(c)$ (kilocalories per mole  $O_{2}$ )

Tempera- ture, K	Mah ( <u>14</u> )	Kellogg ( <u>11</u> )	Ingraham ( <u>7</u> )	Turkdogan, Olsson, and Vinters ( <u>25</u> )	Skeaff and Espelund ( <u>20</u> )	This investigation
971.2	46.795	46.504	ND	ND	ND	53,799
1,000	41.850	41,700	ND	ND	48.930	49.022
1,100	25.350	25,138	31.497	34.637	32.628	32.434
1,123	ND	ND	28,633	31.163	28.878	28.623
1,200	ND	20.430	19.048	19.532	18.372	16.894

ND Not determined.

and





X-ray diffraction analyses of electrode products are given in table 5. The results showed no major change in lattice parameters between the reagents and the components in the equilibrated electrode mixtures. The lattice parameter of a solid solution generally changes with the composition up to the saturation limit and then remains constant beyond that point. Further evidence concerning the limited solubility of sulfur in manganese oxides shows that sulfur solubility, as sulfate ions, increases from 0.055 wt pct at 1,133 K to 0.11 wt pct at 1,373 K (25). Consequently, the assumption of unit activity for the condensed phases for reactions 2 and 3 does not introduce any appreciable error in the standard Gibbs energy of formation of MnSO<sub>4</sub> in the temperature range of this investigation.

The standard Gibbs energy of formation of MnSO4 for the reaction

$$Mn(c) + 0.5 S_{2}(g) + 2 O_{2}(g) = MnSO_{4}(c)$$
(20)

was derived from the relationships

$$\Delta G^{\circ}(\text{reaction 12}) = 2\Delta Gf^{\circ}(MnSO_{L}) - 2\Delta Gf^{\circ}(MnO) - 2\Delta Gf^{\circ}(SO_{2})$$
(21)

		Parame			
Sample	Crystal structure	80	b۰	C۰	Card <sup>2</sup>
Reagents:					
Mn0	Cubic	4.445	NAp	NAp	7-230
Mn, 0,	Tetragonal	5.7621	NAp	9.4696	24-734
MnŠ0,	Orthorhombic	5,267	8.046	6.848	11-88
Electrode mixtures:					
MnO <sup>3</sup>	Cubic	4.441±0.02	NAp	NAp	7-230
MnS0, <sup>3</sup>	Orthorhombic	5.26 ± .01	8.04±0.01	6.85±0.01	11–88
Mn <sub>a</sub> O <sup>°</sup> <sup>4</sup>	Tetragonal	5.76 ± .01	NAp	9.46±.02	24-734
MnŠ0, *	Orthorhombic	5.26 ± .01	8.04± .01	6.86±.01	11-88

TABLE 5. - X-ray diffraction analyses of samples for MnSO, cell

NAp Not applicable.

<sup>1</sup>Parametric measurements for reagents were obtained from the literature.

<sup>2</sup>Numbers refer to data file cards of Joint Committee of Powder Diffraction Standards,

International Centre of Diffraction Data, Swarthmore, Pa.

<sup>3</sup>Mixture for MnO ~ MnSO, electrode.

<sup>\*</sup>Mixture for Mn<sub>3</sub>O<sub>4</sub> - MnSO<sub>5</sub> electrode.

NOTE.--X-ray diffraction analyses were performed by R. A. McCune, a research chemist for the analytical laboratory at the Albany Research Center, Bureau of Mines, Albany, OR.

$$\Delta G^{\circ}(\text{reaction } 13) = 3\Delta Gf^{\circ}(MnSO_{\mu}) - \Delta Gf^{\circ}(Mn_{3}O_{\mu}) - 3\Delta Gf^{\circ}(SO_{2}). \quad (22)$$

In equation 21, the standard Gibbs energies of formation of MnO (2),  $SO_2$  (15), and the Gibbs energy of reaction 12 from this investigation, as given in table 3, may be expressed as follows:

$$\Delta Gf^{\circ}(MnO) = -92.050 + 17.50 \times 10^{-3} T \pm 0.150 \text{ kcal/mol} (900-1,000 \text{ K}), \quad (23)$$
  
$$\Delta Gf^{\circ}(SO_2) = -86.545 + 17.47 \times 10^{-3} T \pm 0.050 \text{ kcal/mol} (900-1,200 \text{ K}), \quad (24)$$

and

and

$$\Delta G^{\circ}(\text{reaction 12}) = -164.027 + 112.87 \times 10^{-3} T$$
  
$$\pm 0.122 \text{ kcal } (896.5-946.3 \text{ K}). \tag{25}$$

Rearranging equation 21 and substituting the proper values for the standard Gibbs energy of reaction 12, as given by equation 25,  $\Delta$ Gf° of MnO (2) from equation 23, and  $\Delta$ Gf° of SO<sub>2</sub> (15) from equation 24 yields

$$\Delta Gf^{\circ}(MnSO_4) = -260.609 + 91.41 \times 10^{-3}T \pm 0.169 \text{ kcal/mol} (896.5-946.3 \text{ K}).$$
 (26)

In equation 22, the standard Gibbs energy of formation of  $Mn_3O_4$  (19) and the standard Gibbs energy of reaction 13 from this investigation, as given in table 4, may be expressed as

$$\Delta Gf^{\circ}(Mn_{3}O_{4}) = -329.326 + 79.46 \times 10^{-3} T \pm 0.453 \text{ kcal/mol} (746.9-1,208.6 \text{ K}), (27)$$

$$\Delta G^{\circ}(\text{reaction 13}) = -214.913 + 165.89 \times 10^{-3} T \pm 0.226 \text{ kcal} (971.2-1,123 \text{ K}), (28)$$

and 
$$\Delta G^{\circ}(\text{reaction 13}) = -199.690 + 152.33 \times 10^{-3} T$$
  
 $\pm 0.372 \text{ kcal } (1,123-1,226.8 \text{ K}).$  (29)

Rearranging equation 22 and substituting the values of  $\Delta Gf^{\circ}$  of  $Mn_3O_4$  from equation 27,  $\Delta G^{\circ}$  of reaction 13 from equation 28 or 29, and  $\Delta Gf^{\circ}$  of  $SO_2$  from equation 24 yields the standard Gibbs energy of formation of  $MnSO_4$ , which may be expressed by the linear equations

$$\Delta Gf^{\circ}(MnSO_{4}) = -267.958 + 99.25 \times 10^{-3}T \pm 0.176 \text{ kcal/mol}; (971.2-1,123 \text{ K}) (30)$$

and

$$\Delta Gf^{\circ}(MnSO_{4}) = -262.884 + 94.73 \times 10^{-3}T$$
  

$$\pm 0.202 \text{ kcal/mol} (1,123-1,226.8 \text{ K}). \quad (31)$$

A phase change in  $MnSO_4$  occurs at 1,123 K. An enthalpy of approximately 15.223 $\pm$ 0.226 kcal for reaction 13 or 5.074 kcal/mol  $MnSO_4$  is associated with this transition. This value compares with 10.850 $\pm$ 1.220 kcal/mol,which has been reported in the literature (20) and was also obtained from emf measurements.

A third-law analysis using the Gibbs energy of formation of  $MnSO_4$  from equation 30, combined with entropy and enthalpy data for Mn (6),  $O_2$  (15), rhombic sulfur (9-10), and  $MnSO_4$  (9-10) yields a standard enthalpy of formation of  $MnSO_4$ ,

$$\Delta Hf_{298}^{\circ} = -257.674 \pm 0.20 \text{ kcal/mol}, \qquad (32)$$

where the standard states are pure crystalline Mn and MnSO<sub>4</sub>, gaseous O<sub>2</sub> at unit fugacity, and rhombic sulfur. The calculated value  $-257.674\pm0.20$  kcal/mol compares with  $-254.18\pm0.250$  kcal/mol, which was obtained by solution calorimetry (21) and has been reported in three compilations (11, 14, 26). Calorimetric data were presumably from measurements of stoichiometric MnSO<sub>4</sub> and should provide excellent standard-state data. Unfortunately, the standard-state properties may be quite different from the actual properties of MnSO<sub>4</sub> that is in equilibrium with MnO or Mn<sub>3</sub>O<sub>4</sub>.

These discrepancies between the hypothetical standard-state and actual equilibrium properties are probably related to the defect structure of MnO crystal that was discussed in a recent publication (19). Prediction of chemical behavior of a system by means of thermodynamic data for the hypothetical standard-state composition can be seriously in error at high temperatures if the homogeneous range of each phase is not taken into consideration. Calculation of the Gibbs energy change in going from the standard composition to the actual equilibrium composition corresponds to knowing the activity coefficient as a function of composition within the homogeneous range. Since the equilibrium behavior can vary considerably with composition, the degree of nonstoichiometry must be specified to fix the chemical behavior of the compound. Consequently, any calculations of the dissociation temperatures, pressures, and Gibbs energies for the Mn-S-O system that are based on calorimetric data for  $MnSO_4$  and  $Mn_3O_4$  should be regarded as crude estimates for the actual equilibrium conditions at high temperatures. Standard Gibbs energy changes for reaction 13, which are derived from actual oxygen pressures (equation 10 or 11), are considered to be a more realistic characterization of the actual equilibrium conditions for defining the coexistence of  $Mn_3O_{\mu}$  and  $MnSO_{\mu}$  than are the calorimetric data.

## 2CdO+CdSO4

The equilibrium oxygen pressure and corresponding Gibbs energy change for the CdO-2CdO\*CdSO<sub>4</sub>-SO<sub>2</sub>-O<sub>2</sub> system were determined by measuring the open-circuit potentials for the cell

where the partial pressure of  $0_2'$  at the reference electrode is 0.00922 atm and  $SO_2$  is at 1 atm. The overall cell reaction is

$$6CdO(c) + 2SO_2(g) + O_2(g, 0.0092 \text{ atm}) = 2[2CdO \cdot CdSO_h](c).$$
 (33)

Potential measurements from four cells that were used for the  $2CdO^*CdSO_4$  determination are given in table 6. These results may be expressed as a function of temperature by the linear equation and standard error of estimate

$$E = 1.945.99 - 1.47048T \pm 2.12$$
 (1.036.8-1,208.2 K), (34)

where E is in millivolts. Potential measurements and their corresponding smooth values, derived from equation 34, are given in columns 3, 4, 7, and 8 of table 6. Representative emf-versus-temperature data are illustrated in figure 5.

The equilibrium oxygen pressure,  $pO_2$ , and the corresponding Gibbs energy change for reaction 33 are obtained by the method previously described for reaction 7. Rearranging equation 8 and substituting the value of  $pO_2^{\prime}$ , the partial pressure of

	Tempera-	Ε,	٣٧		Tempera	Ε,	mv
Measurement	ture, K	Measured <sup>1</sup>	Calculated <sup>2</sup>	Measurement	ture, K	Measured	Calculated
1	1,036.8	419.11	421.40	21	1,145.6	265.15	261.41
2	1,037.1	419.31	420.96	22	1,146.3	262.94	260.38
3	1,037.6	420.21	420.22	23	1,147.1	258.35	259.20
4	1,059.2	386.58	388.46	24	1,158.2	236.48	242.88
5	1,060.1	387.08	387.13	25	1,166.6	232.01	230.53
6	1,060.2	388.28	386.99	26	1,166.8	227.91	230.23
7	1,060.6	387.38	386.40	27	1,167.2	226.12	229.65
8	1,081.1	354.75	356.25	28	1,169.1	226.91	226.85
9	1,082.0	355.05	354.93	29	1,179.5	208.44	211.56
10	1,082.3	356.55	354.49	30	1,187.0	198.47	200.53
11	1,082.3	355.85	354.49	31	1,187.0	202.57	200,53
12	1.103.5	321.81	323.32	32	1,187.0	200.87	200.53
13	1,103.9	324.51	322.73	33	1,187.6	198.41	199.65
14	1,104.0	323.42	322.58	34	1,187.9	198.67	199.21
15	1,122.4	296.30	295.52	35	1,188.6	197.45	198.18
16	1,125.2	294.38	291.41	36	1,189.3	197.94	197.15
17	1,125.3	292.98	291.26	37	1,206.3	172.03	172.15
18	1,125.4	293.38	291.11	38	1,207.0	174.43	171.12
19	1,144.4	260.54	263.17	39	1,207.9	169.63	169.80
20	1,145.4	262.54	261.70	40	1,208.2	170.63	169.36

TABLE 6. - Electromotive force (E) of cell Pt,  $2Cd0 \cdot CdS0_{4}$ , Cd0, S0, (g, 1 atm)//Zr0,//0, (g, 0.00922 atm), Pt

<sup>1</sup> Average of 2 measurements ( $\pm$ 0.05 mv) taken at 15-min intervals and corrected for cell calibration. <sup>2</sup> Calculated from linear equation:

 $E = 1,945.99 - 1.47048T \pm 2.12.$ 



for  $2CdO \cdot CdSO_{4}$  reaction.

 $0_2^2$  at the reference electrode, and E from equation 34 yields

$$\log pO_2 = -\frac{39,231}{T} + 27.61.$$
(35)

Figure 6 illustrates the thermodynamic stability of the Cd-S-O system where Cd0 and 2CdO CdSO<sub>4</sub> coexist in the temperature range 1,036.8 to 1,208.2 K. These values of pO<sub>2</sub> are the key for computing the standard Gibbs energy change for the reaction

$$6Cd0(c) + 2SO_2(g) + O_2(g) = 2[2Cd0 \cdot CdSO_4](c)$$
(36)

from the relationship

$$\Delta G^{\circ}(\text{reaction 36}) = -RT \ln K_{36} = RT \ln pO_2 + 2RT \ln pSO_2, \quad (37)$$

where  $K_{36}$ ,  $pO_2$ , and  $pSO_2$  are the equilibrium constant and the equilibrium pressures of  $O_2$  and  $SO_2$  for reaction 36. The equilibrium oxygen pressure is from equation 35, and  $pSO_2$  is derived by the method previously described in equations 16 through 19. The condensed phases in reaction 36 are assumed to have unit activity.

The average total pressure of the system for the  $2Cd0^{\circ}CdSO_4$  measurements is 0.99947 atm. Calculations show that  $pSO_2$  ranges from 0.99946 atm at 1,036.8 K to 0.99577 atm at 1,208.2 K. Consequently, in the temperature range of this investiga-





tion, the standard Gibbs energy for reaction 36, as given by equation 37, is not appreciably affected by the slight variation of  $pSO_2$  from standard conditions. Results of the measurements for  $pO_2$  and the corresponding values of  $pSO_2$ and Gibbs energies for reaction 36 are given in table 7 and illustrated in figure 7.

X-ray diffraction analyses of electrode products are given in table 8.

TABLE 7. - Standard Gibbs energy change for  $6CdO(c) + 25O_2(g) + O_2(g) = 2[2CdO \cdot CdSO_k](c)$ 

Tempera- ture, K	p50 <sub>2</sub> , atm	p0 <sub>2</sub> , atm	-∆G°, kcel/mol O <sub>z</sub>
1,036.8	0.99946	$5.9030 \times 10^{-11} \\ 8.9117 \times 10^{-9} \\ 3.1000 \times 10^{-7} \\ 8.2600 \times 10^{-6} \\ 1.3770 \times 10^{-5} \\ \end{cases}$	48.528
1,100.0	99941		40.545
1,150	99925		34.251
1,200	99873		27.916
1,208.2	998576		26.880



 $= 2[2CdO*CdSO_{4}](c).$ 

TABLE	8.	÷	X-ray	diffraction	analyses	for	2CdO·CdSO	cell
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		Parametric measurements, A <sup>1</sup>			
Sample	Crystal structure	a	b •	Co	Card <sup>2</sup>
Reagents:					
Cd0	Cubic	4.6953	NAp	NAp	5-640
2Cd0+CdS0,	Orthorhombic	6.97	23.34	6.85	26-382
Electrode mixture:					
Cd0 2Cd0*CdS0,	Cubic Orthorhombic	4.695±0.001 6.95 ± .01	NAp 23.29±0.03	NAp 6.84±0.01	5-640 26-382

NAp Not applicable.

<sup>1</sup>Parametric measurements for reagents were obtained from the literature.

<sup>2</sup>Numbers refer to data file cards of Joint Committee of Powder Diffraction Standards,

International Centre of Diffraction Data, Swarthmore, Pa.

NOTE.--X-ray diffraction analyses were performed by R. A. McCune, a research chemist for the analytical laboratory at the Albany Research Center, Bureau of Mines, Albany, OR.

The results showed no major change in lattice parameters between the reagents and the components in the equilibrated electrode mixture. Consequently, intersolubility of the condensed components in the CdO +  $2CdO \cdot CdSO_4$  electrode mixture is negligible and the assumption of unit activity for the condensed phases in reaction 36 does not introduce any appreciable error in the standard Gibbs energy of formation of  $2CdO \cdot CdSO_4$ .

The standard Gibbs energy of formation of 2CdO.CdSO4 for the reaction

$$3Cd(l, g) + 0.5 S_2(g) + 3 O_2(g) = 2CdO \cdot CdSO_4(c)$$
 (38)

....

was derived from the relationship

$$\Delta G^{\circ}(\text{reaction } 36) = 2\Delta G f^{\circ}(2CdO \cdot CdSO_{\mu}) - 6\Delta G f^{\circ}(CdO) - 2\Delta G f^{\circ}(SO_{2}).$$
(39)

In equation 39, the standard Gibbs energies of formation of CdO (16),  $SO_2$  (15) from equation 24, and the standard Gibbs energy of reaction 36 from this investigation, as given in table 7, may be expressed as follows:

$$\Delta Gf^{\circ}(CdO) = -85.659 + 47.21 \times 10^{-3}T \pm 0.200 \text{ kcal/mol} (1,000-1,200 \text{ K}), \quad (40)$$
  
$$\Delta G^{\circ}(\text{reaction 36}) = -179.475 + 126.30 \times 10^{-3}T \pm 0.196 \text{ kcal} (1,036.8-1,208.2 \text{ K}). \quad (41)$$

Rearranging equation 39 and substituting the standard Gibbs energy of reaction 36 from equation 41,  $\Delta$ Gf° of SO<sub>2</sub> from equation 24, and  $\Delta$ Gf° of CdO from equation 40, yields a standard Gibbs energy of formation of 2CdO<sup>•</sup>CdSO<sub>4</sub> for reaction 38, which may be expressed as

$$\Delta Gf^{\circ}(2Cd0 \cdot CdS0_{4}) = -433.260 + 222.25 \times 10^{-3} T$$
  
$$\pm 0.610 \text{ kcal/mol} \quad (1,036.8-1,208.2 \text{ K}). \quad (42)$$

No experimental entropy and enthalpy data are available for  $2CdO^{\circ}CdSO_{4}$ ; consequently, a third-law analysis from experimental data cannot be made. Assuming that  $\Delta H^{\circ}$  and  $\Delta S^{\circ}$  remain fairly constant in the temperature range 1,036.8 to 1,208.2 K, the enthalpy and entropy for reaction 38 at 1,122.5 K, according to the first and second constants in equation 42, are

$$\Delta Hf^{\circ} = -433.260 \pm 0.610 \text{ kcal/mol}$$
(43)

and

$$\Delta Sf^{\circ} = -222.25 \text{ cal/mol} \cdot K.$$
 (44)

The standard states at 1,122.5 K are pure gaseous cadmium at unit fugacity, crystalline  $2CdO^{\circ}CdSO_{i_4}$ , and gaseous  $S_2$  and  $O_2$  at unit fugacity.

#### SUMMARY AND CONCLUSIONS

Equilibrium oxygen pressures for the  $MnO-MnSO_4-SO_2-O_2$ ,  $Mn_3O_4-MnSO_4-SO_2-O_2$ , and  $CdO-2CdO^{\circ}CdSO_4-SO_2-O_2$  systems were measured by a high-temperature emf method using stabilized  $ZrO_2$  as the solid electrolyte. The emf measurements yielded standard Gibbs energies of formation of  $MnSO_4$  and  $2CdO^{\circ}CdSO_4$  from their oxides. The data for  $MnSO_4$  were compared with previously reported measurements, and discrepancies were discussed. No previous Gibbs energies of formation have been reported for  $2CdO^{\circ}CdSO_4$  to permit direct comparison. Standard thermodynamic properties of  $MnSO_4$  were derived by combining results from this investigation with auxiliary data from the literature.

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